



ANNALES DE L'INSTITUT FOURIER

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Kummer-Artin Schreier-Witt family of curves”**

Tome 75, n° 5 (2025), p. 1899-1900.

<https://doi.org/10.5802/aif.3723>

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Les *Annales de l'Institut Fourier* sont membres du
Centre Mersenne pour l'édition scientifique ouverte
www.centre-mersenne.org e-ISSN : 1777-5310

CORRIGENDUM TO “THE RELATIVE CANONICAL IDEAL OF THE KUMMER-ARTIN SCHREIER-WITT FAMILY OF CURVES”

Annales de l’Institut Fourier, vol. 73 (2023), no 3, 1085-1113

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ABSTRACT. — We correct a few typographical errors and ambiguities in the above mentioned published paper.

RÉSUMÉ. — Nous corrigeons quelques erreurs typographiques et ambiguïtés dans l’article publié mentionné ci-dessus.

Dr. Bernhard Köck, who we wish to thank, kindly pointed to us a few typographical errors and ambiguities, which we address below.

- Page 1088, diagram: the labels of all vertical downwards pointing arrows should be $\otimes_R R/\mathfrak{m}_R$ instead of $\otimes_R R/\mathfrak{m}$.
- Page 1092, line before eq. (3.1): $\mathcal{X}_0$ should be replaced by $\mathcal{X}_0/K$.
- Page 1092, line after eq. (3.1): add the sentence “while we let $\mathcal{X}_0/k$ be the curve corresponding to the extension of the rational function field $k(x)$ given by $X^p - X = x^{\ell-pq}$.”
- Page 1092, next sentence beginning with “Bertin-Mézard”: replace “curve above” by “curve $\mathcal{X}_0/K$ ”.
- Page 1093, diagram (3.3): the labels of all vertical downwards pointing arrows should be $\otimes_R R/\mathfrak{m}_R$ instead of $\otimes_R R/\mathfrak{m}$. Moreover $I_{\mathcal{X}_0}$ should be $I_{\mathcal{X}_0/k}$ both in diagram (3.3) and in the line right below.
- Pages 1093-1094, Theorem 3.2: Replace $I_{\mathcal{X}_0}$ by $I_{\mathcal{X}_0/k}$ once in the statement and four times in the proof of Theorem 3.2.
- Page 1095, line after eq. (4.1): replace “on the special fiber” by on “ $\mathcal{X}_0/K$ ”. Next line replace $\Omega_{\mathcal{X}_0/k}$ by $\Omega_{\mathcal{X}_0/K}$.

Keywords: Relative curves, Canonical ideal, Reduction and Lifting.
2020 Mathematics Subject Classification: 14H10, 14F10.

- Page 1095, last paragraph: replace k by K in three instances (first, fourth and last line of paragraph).
- Page 1104, line after eq. (5.1): add “ $\mathcal{X}_0/k$ (given by $X^p - X = x^{\ell-pq}$) and” after “special fiber”.
- Page 1104, eq. (5.1): change $\mathcal{X}_0$ to $\mathcal{X}_0/K$.
- Page 1107, line after diagram 5.1: add “ $\subset R[\{W_{N,\mu}\}]$ ” after “ G_2^c ”.
- Page 1107, last line: change $I_{\mathcal{X}_0}$ to $I_{\mathcal{X}_0/k}$.
- Pages 1108 to 1110: throughout Section 5.1 replace k by K and $I_{\mathcal{X}_0}$ by $I_{\mathcal{X}_0/K}$.
- Page 1109, Remark 5.7: change to “... follows by verifying directly that $\phi_{0,\bar{c}}(G_2^c) = 0$ ”.
- Page 1109, line after Remark 5.7: add “considered over K ” after “Definition 4.3”.
- Page 1111: start the proof with the sentence “The arguments used in the proofs of Proposition 5.6 and Theorem 5.10, when $x_i = 0$ for $1 \leq i \leq q-1$ (and $i = q$ if applicable) imply that $\langle (G_1^c \otimes_R k) \cup (G_2^c \otimes_R k) \rangle = I_{\mathcal{X}_0/k}$.”

BIBLIOGRAPHY

- [1] H. CHARALAMBOUS, K. KARAGIANNIS & A. KONTOGEORGIS, “The relative canonical ideal of the Kummer–Artin Schreier–Witt family of curves”, *Ann. Inst. Fourier* **73** (2023), no. 3, p. 1085–1113.

Manuscrit reçu le 30 mai 2024,
révisé le 5 septembre 2024,
accepté le 7 octobre 2024.

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